

Total No. of Questions : 7]

SEAT No. :

P1423

[Total No. of Pages :2

[5222] - 11

M.Sc.

PHYSICS

PHY UTN- 501: Classical Mechanics

(Semester -I) (2008 Pattern) (Credit System)

Time : 3 Hours]

[Max. Marks :80

Instructions to the candidates:

- 1) *Question No.1 is compulsory, and any four from the remaining.*
- 2) *Draw neat diagram wherever necessary.*
- 3) *Figures to the right indicates full marks.*
- 4) *Use of log table & calculator is allowed.*

Q1) Attempt any four of the following:

- a) Show that Lagrangian for a relativistic particle moving through a potential $v(r)$ is given by $L(\vec{r}, \vec{v}) = -mc^2 \sqrt{1 - v^2/c^2} - V(\vec{r})$ [4]
- b) Explain the concept of generalised coordinates [4]
- c) Explain the effect of Coriolis force on cyclones & anticyclones [4]
- d) Evaluate the following Poisson's bracket $[\vec{a}, \vec{b}]$, where \vec{a} & \vec{b} are constant vectors [4]
- e) Compare Newtonian & Lagrangian formulation [4]
- f) State different properties of central force [4]

Q2) a) Show that the following transformations are canonical [8]

i) $Q = \bar{P}^1$ $P = qp^2$

ii) $Q = q \tan p$ $P = \log(\sin p)$

- b) With the help of example explain the concept of constraint & degrees of freedom [4]
- c) What do you mean by closure & stability of orbits under central forces? State their necessary conditions. [4]

P.T.O.

Q3) a) Solve the problem of simple pendulum by using Hamilton's equation of motion. Show that the phase space is an ellipse [8]

b) State & prove any four properties of Poisson's bracket [8]

Q4) a) Show that the shortest distance between two points in a plane is straight line [8]

b) Obtain a Lagrangian & Solve the Lagrange's equation of motion for a planet moving around the sun in an elliptical orbit. [8]

Q5) a) Define virial of the system. Using virial theorem obtain Boyle's law. [8]

b) Show that Lagrange's equation of motions are invariant under Galilean transformation. [8]

Q6) a) State & prove Poisson's first theorem . [8]

b) Show that the period of rotation of the plane of oscillation of Foucault's pendulum is given by $T = \frac{2\pi}{\omega \sin \lambda}$ [8]

Q7) a) Obtain Hamiltonian for following Langrangians

i) $L(x, \dot{x}) = \frac{1}{2} \dot{x}^2 - \frac{1}{2} w^2 x^2 - \alpha x^3 + \beta x \dot{x}^2.$

ii) $L(r, \dot{r}) = \frac{1}{2} \mu (\dot{r}^2 + r^2 \dot{Q}^2) - \frac{k}{r}$ [8]

b) Draw a phase space & state space for one dimensional harmonic oscillator [4]

c) Show that

$$[u, q_i] = -\frac{\partial u}{\partial p_i} \quad \& \quad [u, p_i] = \frac{\partial u}{\partial p_i} \quad [4]$$

& & &

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SEAT No. :

P1424

[5222]-12

[Total No. of Pages : 2

M.Sc. - I

PHYSICS

PHYUTN - 502 : Electronics

(2008 Pattern) (Semester - I)

Time : 3 Hours]

[Max. Marks : 80

Instructions to the candidates:

- 1) Question No. 1 is compulsory. Attempt any four from the remaining.
- 2) Draw neat diagrams wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Use of logarithmic tables and non-programmable calculator is allowed.

Q1) Attempt any four of the following.

- a) State atleast four parameters of an op-amp and explain any two in detail. [4]
- b) What is PLL? Draw it's block diagram. Define it's capture range and locking range. [4]
- c) What are shift registers? How are they used? State the different types of shift registers. [4]
- d) An op-amp is used in the inverting and non inverting mode with $R_1 = 2K\Omega$ and $R_F = 100K\Omega$. If $V_{cc} = \pm 15V$ and rms input voltage $V_i = 20mV$; calculate the output voltage in each case. [4]
- e) Design second order Butterworth low pass filter for higher cutoff frequency of 5KHz. [4]
- f) If logic '1' = 16V and '0' = 0V, determine the following for R-2R type DAC. [4]
 - i) Analog output for digital input of 1111
 - ii) Resolution

Q2) a) Draw circuit diagram of an asymmetric astable multivibrator. Explain its operation. Design it to generate a rectangular wave of 80% duty cycle and 1KHz frequency at output.

[Given : $+V_{cc} = +10V$ and $-V_{cc} = -10V$ and $\beta = 0.4$] [8]

- b) With neat block diagram, explain the working of switching regulator. State its advantages and two applications. [8]

P.T.O.

- Q3)** a) Draw circuit diagram of full wave precision rectifier. Explain its action. Derive expression for its output voltage. [8]
- b) Explain the concept of foldback current limiting. How it can be implemented for low-voltage regulator using IC723. [8]
- Q4)** a) Draw circuit diagram of an instrumentation amplifier using three op-amps. [8]
- b) Draw functional block diagram of IC 7495. State its various operating modes. [8]
- Q5)** a) Sketch a block diagram of IC8038. State the function of each component. [8]
- b) Draw circuit diagram of first order Butterworth Low-pass filter and explain. Calculate the cutt-off frequency if $R = K\Omega$ and $C = 0.001 \mu F$. [8]
- Q6)** a) Draw block diagram of 3-pin voltage regulator. Explain function of each block. Design adjustable voltage regulator using LM317 to have an output voltage variable from 5 to 15V. [8]
- b) Given the logic equation $Y = ABC + B\bar{C}D + \bar{A}BC$ make a truth table. Simplify using Karnaugh-map and sketch the necessary logic diagram. [8]
- Q7)** Write short note on any four of the following. [16]
- a) Successive approximation ADC.
 - b) Satellite communication.
 - c) Voltage controlled oscillator using IC566.
 - d) DC to DC converter.
 - e) Function generator using two OPAMPS.
 - f) UPS and Inverters.



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SEAT No. :

P1425

[Total No. of Pages : 3

[5222] - 13

M.Sc.

PHYSICS

PHYUTN-503 : Mathematical Methods in Physics

(2008 Pattern) (Semester - I)

Time : 3 Hours]

[Max. Marks :80

Instructions to the candidates:

- 1) Question No. 1 is compulsory. Attempt any four questions from the remaining.
- 2) Draw neat diagrams wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Use of logarithmic table and calculator is allowed.

Q1) Attempt any four of the following :

- a) Find Laplace transform of $\sinh(at)$. [4]
- b) Let V be the set of ordered pairs of real numbers : $V = \{(a, b); a, b \in \mathbb{R}\}$. Show that V is not a vector space over \mathbb{R} with respect to the following operations of addition in V and scalar multiplication on V :
 $(a, b) + (c, d) = (a, b)$ and $K(a, b) = (ka, kb)$ [4]
- c) State and prove the Parseval's Identity for Fourier series. [4]
- d) Define Basis and Dimension of a vector space. [4]
- e) Prove that : $H_{n+1}(x) = 2xH_n(x) - 2nH_{n-1}(x)$. [4]
- f) Evaluate $\oint_C \frac{e^z}{z(z+1)} dz$ where C is the circle $|z-1|=3$. [4]

- Q2) a) Define Inner product space. Verify that $\langle u, v \rangle = x_1y_1 - x_1y_2 - x_2y_1 + 3x_2y_2$, where $u = (x_1, x_2)$ and $v = (y_1, y_2)$ is an inner product in \mathbb{R}^2 . [8]
- b) Find the Fourier coefficients a_n and b_n in the interval $(-L, +L)$ for odd and even functions. [8]

P.T.O.

Q3) a) Find $L^{-1} \left\{ \frac{5s^2 - 15s + 7}{(s+1)(s-2)^3} \right\}$. [8]

b) Consider the following basis of Euclidean space \mathbb{R}^3 .

$$\{v_1 = (1, 1, 1), v_2 = (0, 1, 1), v_3 = (0, 0, 1)\}$$

By using Gram-Smidt orthogonalization process transform $\{v_i\}$ into an orthonormal basis $\{u_i\}$. [8]

Q4) a) State and prove the orthogonality property of Hermite functions. [8]

b) State and prove Cauchy Riemann equations for a function to be analytic. [8]

Q5) a) Obtain the Associated Legendre functions $P_2^1(x)$ and $P_3^2(x)$. [8]

b) Find Laurent series about the indicated singularity for each of the following functions. Name the singularity in each case and give the region of convergence of each series. [8]

i) $\frac{e^z}{(z-1)^2}; z = 1$

ii) $z \cos \frac{1}{z}; z = 0$.

Q6) a) Let $A = \begin{pmatrix} 1 & -3 & 3 \\ 3 & -5 & 3 \\ 6 & -6 & 4 \end{pmatrix}$. Find a (real) orthogonal matrix P for which $P^{-1}AP$ is diagonal. [8]

b) Obtain the Fourier series corresponding to the function :

$$f(x) = 0, -5 < x < 0$$

$$f(x) = 3, 0 < x < 5, \text{ period} = 10. [8]$$

- Q7)** a) Prove that : $J'_n(x) = \frac{1}{2}[J_{n-1}(x) - J_{n+1}(x)]$. [4]
- b) State and prove Laurent's theorem. [4]
- c) Prove that : $L_{n+1}(x) = 2(n+1-x)L_n(x) - n^2L_{n-1}(x)$. [4]
- d) Determine the region in the z plane represented by $1 < |z+2i| \leq 2$. [4]



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SEAT No. :

P1426

[5222]-14

[Total No. of Pages : 3

M.Sc.

PHYSICS

PHYUTN - 504 : Quantum Mechanics-I
(2008 Pattern) (Semester - I)

Time : 3 Hours]

[Max. Marks : 80

Instructions to the candidates:

- 1) Question No.1 is compulsory and solve any four questions from the remaining.
- 2) Draw neat diagram wherever necessary.
- 3) Figures to the right indicate full marks.
- 4) Use of logarithmic tables and electronic pocket calculator is allowed.

Q1) Attempt any four of the following:

- a) If L and A are linear operators then prove that

$$e^L A e^{-L} = A + [L, A] + \frac{1}{2!} [L, [L, A]] + \dots \quad [4]$$

- b) If an arbitrary state $|\psi\rangle$ is expanded in terms of complete set of eigen functions $|a\rangle$ by an equation $|\psi\rangle = \sum_a C_a |a\rangle$, hence define a projection operator \hat{P}_a . [4]
- c) Using uncertainty relation, estimate the size of hydrogen atom in the ground state. [4]
- d) Write note on Dirac δ -function. [4]
- e) State four postulates of quantum mechanics. [4]
- f) In momentum space, show that $[x_{0p}, P_{0p}] = i\hbar$. [4]

- Q2) a) Obtain coefficients C_{lm}^\pm in equation $L_\pm |l, m\rangle = C_{lm}^\pm |l, m \pm 1\rangle$, where $|l, m\rangle$ are simultaneous eigen states of L^2 and L_z operators and L_+ and L_- are raising and lowering operators. [8]
- b) What is unitary transformation? By using it explain the transformation of one complete orthonormal set of basis to other basis. [8]

P.T.O.

Q3) a) Describe Schrodinger and Heisenberg pictures during the evolution of system with time. [8]

b) i) If \hat{A} and \hat{B} are operators, then prove that [4]

$$1) (A^+)^\dagger = \hat{A}$$

$$2) (\hat{A} \hat{B})^\dagger = \hat{B}^\dagger \hat{A}^\dagger$$

ii) Consider a one - dimensional physical system described by

$$\text{Hamiltonian. } H = \frac{p^2}{2m} + V(x)$$

Then show that $[H, x] = \frac{1\hbar}{m} P$ and for a stationary state find $\langle p \rangle$. [4]

Q4) a) Show that i) $\left(\frac{L_z}{\hbar}\right)$ play a role of the generator of infinite simal rotations and ii) For finite rotations through an angle θ , when $M \rightarrow \infty$ then $\psi'(x) = e^{i\theta \hat{n} \cdot \vec{L} / \hbar} |\psi(x)\rangle$, where N=number of infinitesimal rotations and \hat{n} is unit vector about an arbitrary axis of rotation. [8]

b) Obtain eigen values and eigen functions of simple harmonic oscillator by abstract operator method. [8]

Q5) a) Obtain eigen value spectrum of J^2 and J_z operators. [10]

b) What are observables? Use expansion postulate to show that [6]

i) Eigen functions belonging to discrete eigen values are normalizable and

ii) Eigen - functions belonging to continuous eigen-values are of infinite norm.

- Q6)** a) Write notes on
- i) Matrix representation of an operator. [4]
 - ii) Change of basis. [4]
- b) For a particle of mass m , moving in a 1D potential well of finite width obtain expressions for energy and normalized eigen function. Also write expressions for energy and eigen function for a 2D case. [8]
- Q7)** a) If \bar{A}, \bar{B} are operators which commute with $\bar{\sigma}$ then show that
- $$(\bar{\sigma} \cdot \bar{A})(\bar{\sigma} \cdot \bar{B}) = \bar{A} \cdot \bar{B} + i \bar{\sigma} \cdot (\bar{A} \times \bar{B}) \quad [4]$$
- b) Give physical significance of eigen values, eigen functions and expansion coefficients. [4]
- c) Find the values of $[J_z, J_+], [J_z, J_-], [J_+, J_-]$ and $[J_x, J^2]$. [4]
- d) Prove that eigen values of Hermitian operator are real. [4]



Total No. of Questions :7]

SEAT No. :

P1427

[Total No. of Pages :3

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M.Sc.

PHYSICS

**PHY UTN 601: Electrodynamics
(2008 - Pattern) (Semester - II)**

Time : 3 Hours]

[Max. Marks :80

Instructions to the candidates:

- 1) Question No. 1 is compulsory and solve any four questions from the remaining.*
- 2) Draw neat labelled diagrams wherever necessary.*
- 3) Figures to the right indicate full marks.*
- 4) Use of logarithmic tables and pocket calculator is allowed.*

Q1) Attempt any four of the following:

[16]

- a) Find the skin-depth in sea water with conductivity $\sigma = 5 (\Omega\text{m})^{-1}$ at a frequency 10^{10}Hz . For sea water $\mu = \mu_0 = 4\pi \times 10^{-7}\text{Wb/A-m}$.
- b) Show that the ratio of electrostatic and magnetic energy densities $\left(\frac{u_e}{u_m}\right)$ is equal to unity.
- c) Compute the electric field associated with a LASER beam having energy per unit volume is 100 J/m^3 .
- d) Find the velocity at which the mass of the particle is double it's rest mass. Given: $C = 3 \times 10^8\text{m/sec}$.
- e) Calculate the magnitude of poynting's vector at the surface of the sun. Given that the power radiated by sun is equal to 3.8×10^{26} watt and radius of the sun is equal to $7 \times 10^8\text{m}$.
- f) Explain Minkowski's space - time diagram.

Q2) a) If a medium is moving with a velocity \vec{u} , then show that the Faraday's

law has the form
$$\vec{\nabla} \times (\vec{E}' - \vec{u} \times \vec{B}) = -\frac{\partial \vec{B}}{\partial t}$$

[8]

P.T.O.

b) Show that the operator.

$\square^2 \equiv \nabla^2 - \frac{1}{c^2} \frac{\partial^2}{\partial t^2}$ is invariant under Lorentz transformations.

where as $\nabla^2 \equiv \frac{\partial^2}{\partial x^2} + \frac{\partial^2}{\partial y^2} + \frac{\partial^2}{\partial z^2}$ is not Lorentz invariant. [8]

Q3) a) Explain the term ‘multipole moments’. Hence derive an expression for potential at a distant point using multipole expansion for a localized charge distribution in free-space. [8]

b) Show that $(C^2 B^2 - E^2)$ and $(\vec{E} \cdot \vec{B})$ are invariant under Lorentz transformations. [8]

Q4) a) Explain the term electromagnetic field tensor. Hence obtain an expression for e.m. field tensor $F_{\mu\gamma}$. [8]

b) The magnetic field intensity \vec{B} at a point is given by $\vec{B} = \left(\frac{\mu_0}{4\pi} \right) \int \frac{\vec{j} \times \vec{r}}{r^3} d\tau$.

Show that $\vec{\nabla} \times \vec{B} = \mu_0 \vec{j}$. [8]

Q5) a) What is Hertz potential? Show that the electric and magnetic fields can be expressed in terms of Hertz potential as $\vec{E} = \vec{\nabla} \times (\vec{\nabla} \times \vec{Z})$ and

$\vec{B} = \frac{1}{c^2} \frac{\partial}{\partial t} (\vec{\nabla} \times \vec{Z})$, where \vec{Z} is the Hertz potential. [8]

b) Describe Michelson - Morley experiment with reference to special theory of relativity. Derive the necessary formula for the fringe shift and comment on the result. [8]

Q6) a) Show that the Maxwell’s equations in a charge free region lead to:

$$\nabla^2 \vec{E} - \frac{kk_m}{c^2} \frac{\partial^2 \vec{E}}{\partial t^2} - \mu\sigma \frac{\partial \vec{E}}{\partial t} = 0$$

Explain which term can be ignored in a nonconducting medium. [8]

- b) A plane e.m. wave is incident on an interface between the two non-conducting dielectric media. Obtain expressions for Fresnel's equations if the electric field vectors are perpendicular to the plane of incidence. [8]

- Q7) a) Write Maxwell's equations in differential and integral forms. [4]
- b) Write in short about the electric dipole radiation and explain the term 'radiation resistance'. [4]
- c) Calculate the rest mass energy of an electron in eV if its rest mass is equal to 9.11×10^{-31} kg. [4]
- d) Find the phase velocity of a plane e.m. wave at a frequency of 10 GHz in polyethelene material. [4]

$$\text{Given: } \mu \approx \mu_0 = 4\pi \times 10^{-7} \frac{\text{wb}}{\text{A-m}},$$

$$\epsilon_r = 2.3,$$

$$\epsilon_0 = 8.85 \times 10^{-12} \frac{\text{C}^2}{\text{N-m}^2}$$

$$\text{and } \sigma = 2.56 \times 10^{-4} \frac{\text{mho}}{\text{m}}.$$



Total No. of Questions : 7]

SEAT No. :

P1428

[5222]-22

[Total No. of Pages : 3

M.Sc.

PHYSICS

**PHYUTN - 602 : Atoms, Molecules and Solids
(2008 Pattern) (Semester - II)**

Time : 3 Hours]

[Max. Marks : 80

Instructions to the candidates:

- 1) *Question No. 1 is compulsory. Solve any four questions from the remaining.*
- 2) *Draw neat diagrams wherever necessary.*
- 3) *Figures to the right indicate full marks.*
- 4) *Use of logarithmic tables and electronic calculator is allowed.*

Given :

$$\text{Rest mass of } e = 9.109 \times 10^{-31} \text{ kg}$$

$$\text{Charge on the } e = 1.6021 \times 10^{-19} \text{ Coulomb}$$

$$\text{Planck's constant} = 6.626 \times 10^{-34} \text{ Js}$$

$$\text{Boltzman constant} = 1.38054 \times 10^{-23} \text{ JK}^{-1}$$

$$\text{Avogadro's number} = 6.022 \times 10^{26} (\text{K mole})^{-1}$$

$$\text{Bohr magneton} = 9.27 \times 10^{-24} \text{ amp-m}^2$$

$$1 \text{ eV} = 1.6021 \times 10^{-19} \text{ J}$$

Q1) Solve any four of the following.

- a) A spectral line wavelength 5000\AA when placed in a magnetic field of 10 Tesla, is observed to be a normal Zeeman triplet. Calculate wavelength separation between composition of triplet. **[4]**
- b) The values of $\bar{\gamma}_e$ and x_e for lower and upper states of CO are $2,170.21 \text{ cm}^{-1}$, 0.0062 and $1,515.61 \text{ cm}^{-1}$, 0.0114 respectively. The (0,0) transition is observed at 64746.55 cm^{-1} , calculate the energy difference of the two electronic states. **[4]**
- c) Determine Lande's g factor for ${}^2f_{5/2}$. **[4]**

P.T.O.

- d) The highest possible lattice frequency is $11.85 \times 10^{12} \text{ s}^{-1}$ in case of Silicon. Estimate the Debye temperature for Silicon. [4]
- e) The concentration of Schottky defects in an ionic crystal is 1 in 10^{10} at temperature 500 K. Estimate the energy of the vacancy pair. [4]
- f) Show that the maximum radius of the sphere that can just fit into the void at the body centre of the fcc structure confined by the facial atoms is $0.414r$. Where r is the radius of the atom. [4]
- Q2)** a) What is the geometrical structure factor? Derive an expression for geometrical structure factor for a fcc structure. [8]
- b) Explain in detail the Frankel defects occurring in an crystal. [8]
- Q3)** a) Deduce the expression for the specific heat of a solid based on Debye model. [8]
- b) Discuss the vibrational modes of 1– D monoatomic lattice of identical atoms hence obtain the dispersion relation. [8]
- Q4)** a) In the context of rotational fine structure of electronic vibration spectra explain band origin and band head. [8]
- b) Explain with diagrams the vibrational course structure showing ν'' progression. [8]
- Q5)** a) Explain the principle and working of NMR spectrometer and state its applications. [8]
- b) State and explain Frank-Condon principle. [8]
- Q6)** a) Explain the experimental arrangement to study normal Zeeman effect. Derive the formula for change in wavelength. [8]
- b) Explain Screw and Edge dislocations in solids. [8]

- Q7)** a) Obtain expression for configurational entropy. [4]
- b) What is line broadening. State the factors responsible for broadening of spectral line. [4]
- c) What are normal and Umklapp processes. [4]
- d) What is Phonon? Its role on quantization of elastic waves. [4]



Total No. of Questions :7]

SEAT No. :

P1429

[5222]-23

[Total No. of Pages : 3

M.Sc.

PHYSICS

**PHY UTN - 603 : Statistical Mechanics in Physics
(2008 Pattern) (Semester - II)**

Time : 3 Hours]

[Max. Marks : 80

Instructions to the candidates:

- 1) *Question No.1 is compulsory; Solve any four questions of the remaining.*
- 2) *Draw neat diagrams wherever necessary.*
- 3) *Figures to the rightside indicate full marks.*
- 4) *VSC of Logarithmic tables and electronic pocket calculator is allowed.*

Constants:

- 1) *Boltzmann constant, $K_B = 1.38 \times 10^{-23} \text{ J/K}$.*
- 2) *Gas constant $R = 1.987 \text{ cal / deg./mole}$.*
- 3) *Avogadro's number, $N = 6.023 \times 10^{23} \text{ /gm.mole}$.*
- 4) *Planck's constant $h = 6.625 \times 10^{-34} \text{ J.sec}$.*
- 5) *Mass of electron. $m_e = 9.1 \times 10^{-31} \text{ Kg}$*

Q1) Attempt Any Four of the following.

- a) Explain the concept of phase space. **[4]**
- b) A system of 3 particles has energy levels with energies 0,1,2,3 units. The total energy of the system is 3 units. List the accessible microstates if the particles are i) indistinguishable ii) distinguishable. **[4]**
- c) Show that the energy in canonical ensemble can be represented as
$$S = -k \sum P_r \ln P_r$$
 [4]
- d) Compare the basic postulates of B.E. & F.D. statistics. **[4]**
- e) Show that at high temperature Bose-Einstein and Fermi-Dirac distribution reduce to maxwell-Boltzman distribution. **[4]**
- f) Explain, what do you mean by mechanical and thermal interaction. **[4]**

P.T.O.

- Q2) a)** Show that for classical monoatomic ideal gas having N particles contained in volume V . The number of states $\Omega(E)$ to the system in the energy range E & $E + \delta E$ is given by

$$\Omega(E) = BV^N E^{3N/2} \quad [8]$$

- b) For grand canonical ensemble show that probability of finding the system in a particular microstate r having energy E_r and number of particles N_r is given by

$$P_r = \frac{e^{-\beta E_r - \alpha N_r}}{\sum_r e^{-\beta E_r - \alpha N_r}} \quad [8]$$

- Q3) a)** On the basis of canonical distribution, obtain the law of atmosphere
 $P(z) = P(o) e^{-mgz/KT}$ [8]

- b) State the partition function for B.E statistics and obtain the B.E distribution in the form

$$\bar{n}_s = \frac{1}{e^{\beta(\epsilon_s - \mu)} - 1}$$

Where μ is the chemical potential. [8]

- Q4) a)** In case of Bose - Einstein condensation for $T < T_b$, Prove that

$$N = N_0 + N \left(\frac{T}{T_b} \right)^{3/2}$$

Where N = total number of particles

N_0 = number of particles in ground state. [8]

- b) Show that the Fermi energy of fermions is

$$\epsilon_F = \frac{\hbar^2}{2m} \left(\frac{3\pi^2 N}{v} \right)^{2/3} \quad [8]$$

Q5) a) Show that for photons, the mean pressure \bar{P} is related to its total energy \bar{E} by the relation $\bar{P} = \frac{1}{3} \frac{\bar{E}}{V}$ [8]

b) Consider a system of N diatomic molecules each having vibrational energy levels. $E = \left(n + \frac{1}{2} \right) \hbar \omega$.

where $n = 0, 1, 2, 3, \dots$

Write down the partition function and derive an expression for mean energy. Hence show that at low temperature, the specific heat is given by

$$C_v = 3R \left(\frac{\theta_E}{T} \right)^2 e^{-\theta_E/T}. \quad [8]$$

Q6) a) Show that Maxwell's distribution of speed is given by [8]

$$F(v)dv = 4\pi n \left(\frac{m}{2\pi KT} \right)^{3/2} v^2 e^{-\frac{mv^2}{2KT}} dv$$

b) State and prove Liouville's theorem. [8]

Q7) a) State and explain the postulate of equal-a-prior probability. [4]

b) Write a note on white Dwarf. [4]

c) Calculate the mean values \bar{E} and $\overline{E^2}$ for canonical ensemble in terms of partition function. [4]

d) State the equipartition theorem; hence find out mean energy for solid consisting of N molecules. [4]



Total No. of Questions : 7]

SEAT No. :

P1430

[Total No. of Pages : 3

[5222] - 24

M.Sc.

PHYSICS

PHYUT-604 : Quantum Mechanics - II
(2008 Pattern) (Semester - II)

Time : 3 Hours]

[Max. Marks :80

Instructions to the candidates:

- 1) *Question 1 is compulsory.*
- 2) *Attempt any four questions from remaining.*
- 3) *Figures to the right indicate full marks.*
- 4) *Use of calculators is allowed.*

Q1) Attempt any four of the following :

[16]

- a) Discuss the conditions of validity of Born approximation.
- b) One dimensional harmonic oscillator is perturbed by $H' = \lambda x^3$. Obtain the first order correction in energy in first excited state.
- c) Using harmonic perturbation explain induced absorption and spontaneous emission.
- d) Obtain antisymmetric wave functions for a system of two electrons.
- e) List the connection formulae used in WKB approximation.
- f) Obtain the relation between angles of scattering in Laboratory frame and centre of mass frame.

Q2) a) Obtain the expression for scattering amplitude using Green's function. **[8]**

- b) State and prove Fermi Golden rule for the rate of transitions induced by constant potential. **[8]**

P.T.O.

Q3) a) Using trial wave function $\psi(x) = Ae^{-\alpha x^2}$, estimate the ground state energy of harmonic oscillator. α - is variational parameter. [8]

b) A particle of charge q , in simple harmonic motion along x -axis, is acted on by a time-dependent homogeneous electric field.

$$\mathcal{E}(t) = \mathcal{E}_0 \cdot \exp\left(-t^2/\tau^2\right)$$

where \mathcal{E}_0 and τ are constants. If the oscillator is in its ground state at $t = -\infty$, find the probability that it will be found in omitted state as $t \rightarrow \infty$.

$$\left(\text{Use: } \int_{-\infty}^{+\infty} e^{-\alpha u^2} e^{-\beta u} du = \left(\frac{\pi}{\alpha}\right)^{1/2} e^{-\beta^2/4\alpha} \right) \quad [8]$$

Q4) a) Discuss time-independent perturbation theory for a degenerate energy level. [8]

b) Using WKB approximation, obtain expression for transmission coefficient. [8]

Q5) a) Using partial wave analysis, show that the scattering cross-section is given as $\sigma_t = \frac{4\pi}{k^2} \sum_l (2l+1) \sin^2 \delta_l$. [10]

b) Discuss concept of identical particles. Show that exchange operator and Hamiltonian operator commute with each other. [6]

Q6) a) Find the total cross-section for low-energy (s-wave) scattering by a potential barrier such that $V(r) = \begin{cases} -V_0 & \text{for } r \leq a \\ 0 & \text{for } r > a \end{cases}$. [8]

b) Discuss field emission of electrons from a metal using WKB approximation. [8]

- Q7)** a) Explain the selection rules for electric dipole transitions. [4]
- b) Show that the variational method gives an upper bound to the ground state energy. [4]
- c) Explain the collision process between identical particles. [4]
- d) Show the stark effect is zero in the ground state of hydrogen atom. [4]



Total No. of Questions : 7]

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M.Sc.

PHYSICS

PHY UTN- 701: Solid State Physics

(Semester - III) (2008 Pattern)

Time : 3 Hours]

[Max. Marks :80

Instructions to the candidates:

- 1) *Question No.1 is compulsory. Solve any Four questions from the remaining.*
- 2) *Figures to the right indicate full marks.*
- 3) *Draw neat labelled diagram wherever necessary*
- 4) *Use of logarithmic table and scientific calculator is allowed.*

Given:

Rest mass of electron = 9.1×10^{-31} Kg.

Electronic charge = 1.602×10^{-19} C.

Planck's constant = 6.62×10^{-34} J-S.

Boltzmann constant = 1.38×10^{-23} JK⁻¹.

Avogadro's Number = 6.023×10^{26} atoms per kgmole.

Bohr Magneton = 9.27×10^{-24} A-m²

Permeability of free space = $4\pi \times 10^{-7}$ Henry/m

Permittivity of Free space = 8.85×10^{-12} c²/N-m²

Q1) Attempt any four of the following:

[16]

- a) A Copper wire of length 0.5 m and diameter 0.3 mm has a resistance 0.12 Ω at 20°C. If the thermal conductivity of copper at 20°C is 390 Wm⁻¹k⁻¹. Determine Lorentz number.
- b) Show that for a 2- dimensional square Lattice, the kinetic energy of a free electron at a corner of the first Brillouin zone is higher than that of an electron at mid point of a side face of zone by a factor of 2.

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- c) Estimate the temperature at which there is 1% probability that a state with an energy 0.5 eV above the fermi energy will be occupied by an electron.
- d) Determine the critical current which can flow through a long thin super conducting wire of Al of diameter 10^{-3} m. The critical magnetic field for aluminium is 7.9×10^3 A/m.
- e) A magnetic material has a magnetization of 3300 A/m and flux density of 0.0044 wb/m². Calculate the magnetizing force and the relative permeability of the material.
- f) For a He atom in its ground state (1s) , the mean radius in the Langevin's formula may be approximated by the Bohr radius 0.53 nm. Density of He is 0.178 kg/m³. Calculate the diamagnetic susceptibility of He atom,
- Q2)** a) Discuss the nearly free electron model and explain how it leads to the formation of forbidden gap and band structure. [8]
- b) Explain the concept of reduced, extended and periodic zone schemes used for the representation of energy bands with neat diagrams. [8]
- Q3)** a) For an atom placed at general Lattice site, obtain an expression for local electric field E_{local} , Explain physical significance of each term in the expression. [8]
- b) Define dielectric function $\epsilon(\omega, k)$. For the long wavelength region, derive the expression,
- $$\epsilon(\omega) = 1 - \frac{wp^2}{\omega^2},$$
- where symbols have usual meanings. On the basis of plot of this equation explain attenuation of the wave. [8]
- Q4)** a) Explain the equation theory of paramagnetism and obtain Curie law. [8]
- b) Derive London equation for super conducting state and obtain an expression for penetration depth. [8]
- Q5)** a) Discuss the origin of diamagnetism in a free atom. Obtain Langevin's diamagnetism formula. [8]
- b) Distinguish between ferromagnetism, ferrimagnetism and antiferromagnetism. [8]

- Q6)** a) Prove that the entropy of a superconducting material is lesser than that of a normal metal. [8]
- b) Draw a suitable diagram for the hysteresis loop for a magnetic material and explain it with the help of domain theory. [4]
- c) Discuss the term 'Anisotropy Energy' with reference to magnetization. [4]
- Q7)** a) Define Bloch function and write a note on it. [4]
- b) What is Fermi-Dirac statistics. With neat diagram, explain its temperature dependence. [4]
- c) Describe the term 'Bloch wall' with reference to magnetism. [4]
- d) The critical temperature (T_c) for Hg with isotopic mass 199.5 is 4.185 K. Calculate its critical temperature when its isotopic mass changes to 203.4. [4]

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Total No. of Questions :7]

SEAT No. :

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M.Sc.

PHYSICS

PHY UTN 801: Nuclear Physics

(2008 Pattern) (Semester - IV)

Time : 3 Hours]

[Max. Marks :80

Instructions to the candidates:

- 1) *Question No. 1 is compulsory, attempt any four questions from the remaining.*
- 2) *Draw neat figures wherever necessary.*
- 3) *Figures to the right indicate full marks.*
- 4) *Use of logarithmic tables and pocket calculator is allowed.*

Q1) Attempt any four of the following.

[16]

- a) For energy filters in the mass spectrometers, show that $\frac{1}{2}mV^2 = \frac{neVR_o}{2d}$ where symbols carry usual meaning.
- b) Chlorine - 33 decays by positron emission with maximum energy of 4.3 MeV. Calculate the radius of nucleus from this.
- c) Discuss the following reactions using conservation of Isotopic spin.
 - i) $P + P \rightarrow P + P + \Pi^0$
 - ii) $\Pi^+ + P \rightarrow \Pi^+ + P$
- d) Explain weak and strong interactions with suitable examples with reference to elementary particles.
- e) Explain the concept of isospin associated with elementary particle.
- f) Calculate the half value thickness of β absorption in Aluminium for β spectrum with $E_{\max} = 1.17$ MeV. Given = Density of Aluminium = 2700 kg/m³.

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- Q2)** a) What is straggling? Derive the formula for straggling when a charged particle is moving through the matter. [8]
- b) What are quarks? Explain how quarks are treated as Building blocks of hadrons and mesons? [8]
- Q3)** a) Explain important features of Gamow's theory of α decay. [8]
- b) Explain the concept of quadropole moment and derive an expression for the same and show that it is zero for spherical distribution of charges. [8]
- Q4)** a) Draw a diagram of the electron synchrotron accelerator state its working principle and action. Explain how maximum energy of the electron depends on the radius of orbit. [8]
- b) With the help of suitable diagram describe the construction and working of Bainbridge and Jordan Mass spectrometer. [8]
- Q5)** a) Explain the working of proportional counter. state its advantages and applications. [8]
- b) For p - p scattering at low energies, derive an expression for differential cross section in Laboratory system. [8]
- Q6)** a) Derive Bethe's formula for 'stopping power' of charged particles moving through the matter. Write the expression for relativistic effects. [8]
- b) Write a note on Graphite moderated Reserach Reactor. [4]
- c) Verify the following reaction and state whether it is allowed or forbidden on the basis of laws of conservation of strangeness, baryon number and charge. $\Pi^+ + P \rightarrow \Lambda^0 + k^0$. [4]

- Q7)** a) Explain weak and strong interactions with suitable examples with reference to elementary particles. [4]
- b) Write a short note on mirror nuclei. [4]
- c) Explain the concept of ISO - spin associated with elementary particles. [4]
- d) Discuss in brief production and properties of pion. [4]

